

Reading: Boas on Fourier Series: Chapter 7 sections 1 - 3, 5 and 7 (Boas covers this in detail, more than we will in 320.)

- (1) Boas pg 355 number 5
- (2) Let's use the basis functions

$$\langle x | n \rangle = \frac{1}{\sqrt{\pi}} \cos(nx)$$

on $-\pi < x < \pi$. (n is an integer.) The inner product is

$$\langle u | v \rangle = \int_{-\pi}^{\pi} u^*(x)v(x)dx$$

so the weighting function is 1 and all these functions are real. Suppose you have a ket $|v\rangle$ which is the function

$$\langle x | v \rangle = 2 \cos x + \cos(2x).$$

- (a) Find $\langle 1 | v \rangle$.
- (b) Find $\langle n | v \rangle$ for any n .

Feel free to solve this by inspection.

- (3) A very handy feature of Mathematica is the command `BesselJZero`, useful for instance on finding the modes of a circular drum head as Spencer mentioned.
 - (a) Plot $J_1(x)$ from 0 to 12.
 - (b) Find the first 4 zeros of $J_1(x)$. (Using `N[BesselJZero . . .]` will give a numerical evaluation.)