

Reading: Boas: We will be reading Chapter 10 on tensors but for now the better thing would be to flip through this to see how the chapter is organized.

(1) Index work:

(a) With vector

$$v^i \xrightarrow{\mathcal{O}} (1, -1), \text{ and one form } \omega_j \xrightarrow{\mathcal{O}} (a, b)$$

where a and b are constants. Find the scalar $v^i \omega_i$.

(b) With metric

$$g_{ij} \xrightarrow{\mathcal{O}} \begin{pmatrix} F & 1 \\ 1 & 0 \end{pmatrix}$$

find the dual vector $v_j = v^i g_{ij}$

(c) Find the tensor $v^i \omega^j$.